METHOD AND APPARATUS TO RELATE BIOMETRIC SAMPLES TO TARGET FAR AND FRR WITH PREDETERMINED CONFIDENCE LEVELS

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This patent is subject to a terminal disclaimer.

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G10L 17/00 (2006.01)

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Field of Classification Search ............... 382/115; 713/186; 340/5.8; 902/3
See application file for complete search history.

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ABSTRACT
At least two biometric measurements of a person are collected, then a statistical measure based on the measurements is computed. The statistical measure is a bounded estimate of the discriminative power of a test based on the measurements. While the discriminative power is less than a target value, additional biometric measurements are collected. When enough measurements have been collected, a biometric template is constructed from the measurements and stored for use in future identifications. Systems and software to implement similar methods are also described and claimed.

20 Claims, 3 Drawing Sheets
<table>
<thead>
<tr>
<th>U.S. PATENT DOCUMENTS</th>
<th>OTHER PUBLICATIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>2006/0018523 A1 1/2006 Saitoh et al.</td>
<td>PENN STATE RESEARCH FOUNDATION, Final office action</td>
</tr>
</tbody>
</table>
Collect Plurality of Biometric Samples

Compute Upper Bound of Error Variance

Compute Estimated Number of Additional Samples Required to Enroll

More Samples Required?

Yes

Display Estimated Number

Collect Supplemental Biometric Sample

No

Done
METHOD AND APPARATUS TO RELATE BIOMETRIC SAMPLES TO TARGET FAR AND FRR WITH PREDETERMINED CONFIDENCE LEVELS

CROSS-REFERENCE TO RELATED APPLICATION


FIELD

The invention relates to training biometric authentication systems. More specifically, the invention relates to selecting an adequate number of training samples to achieve a desired level of authentication performance, and evaluating the level of authentication performance that may be expected from a set of training samples.

BACKGROUND

Biometric identification and authentication systems measure physical and/or behavioral characteristics of a person and compare the characteristics to an earlier-prepared sample or “template” to determine whether the measurements were taken from the same person. This determination can be used to control access to tangible or intangible assets and resources on a per-person basis. Other systems based on a physical or informational key (e.g. an actual key, an electronic identification card, or a password) cannot restrict access to a particular person, since the person can transfer the key or password to someone else.

The measurements taken by a biometric system typically vary slightly at each measurement, so the comparison process must accommodate such slight variances. The accuracy of a biometric identification is inversely proportional to the amount of variability tolerated in a set of measurements: if more variability is permitted in measurements, then it becomes easier for an impostor to fool the system. On the other hand, as the permissible variability is reduced, legitimate users are more likely to be rejected due to normal measurement variances. Two key metrics describing the performance of a biometric identification system are the false reject ratio (“FRR” or “α”, the probability of legitimate user erroneously being rejected as an impostor), and the false accept ratio (“FAR” or “β”, the probability of an impostor erroneously being identified as a legitimate user). Administrators of biometric identification systems often tune the system’s parameters to achieve a FAR and FRR that balance the security requirements of the resource protected by the system against the inconvenience to legitimate users of erroneous rejections.

One difficulty encountered in operating a biometric identification system is that of enrolling users into the system. Because of the previously-mentioned measurement variances, many systems require a new enrollee to provide a large number of measurement samples so the system can build a template that will permit accurate identifications later. Providing many samples can be tedious or inconvenient for the new user. Formal methods of evaluating samples to determine when “enough” have been collected, and of estimating identification performance that may be expected given a set of samples, may improve the usefulness and convenience of biometric identification systems.

BRIEF DESCRIPTION OF DRAWINGS

Embodiments are illustrated by way of example and not by way of limitation in the figures of the accompanying drawings in which like references indicate similar elements. It should be noted that references to “an” or “one” embodiment in this disclosure are not necessarily to the same embodiment, and such references mean “at least one.”

FIG. 1 illustrates one method for collecting biometric measurements of a user. The measurements can serve as input to an embodiment of the invention.

FIG. 2 is a flow chart of operations according to an embodiment of the invention.

FIG. 3 shows a data processing system including physical and logical elements that implement an embodiment of the invention.

DETAILED DESCRIPTION

This disclosure presents an analysis of variance-based methods to estimate the number of samples required to achieve a desired level of discriminative performance from a biometric-measurement-based identification system. Formal mathematical methods are used to explain the operation of systems and methods according to embodiments of the invention.

For concreteness, the following discussion will focus on keystroke or typing rhythm patterns as the biometric measurement source. However, it will be apparent to those of ordinary skill in the relevant arts that the methods discussed here can be applied to other biometric measurements, such as fingerprint images, hand geometry measurements, voice recordings, iris and retina patterns, and other similar data.

FIG. 1 shows some data that can be collected as a user types characters on a keyboard. The characters typed in the example depicted are those of password 110, “Gamma 3”. Trace lines 131-136 indicate the press/release state of keyboard keys 121-126, respectively. Time measurements are taken as each key is pressed (140) and released (150). Derivative timing measurements such as the time between consecutive key presses (160) or consecutive key releases (170) may also be computed from key press and key release times and included in a biometric measurement.

Note that typing a multi-character string once results in the generation of a plurality of timing measurements. In this disclosure, a single “biometric measurement” is considered to be a plurality of scalar quantities. It is convenient to think of a biometric measurement as a vector. In accordance with common academic practice, vectors will be indicated by bold, upper-case letters (e.g. “Y”), while the scalar quantities that make up a vector are indicated by subscripted, upper-case, italic letters (e.g. “Y_i”). One of a plurality of biometric measurements will be indicated as a subscripted vector (e.g. “Y_2”). One scalar quantity out of a plurality of biometric measurement vectors will be indicated as “Y_i” (the jth scalar quantity of the ith biometric measurement vector).

Biometric measurement values are modeled as

\[ Y_i = \mu_i + \sigma_i \]  

where \( 1 \leq i \leq n \) (the number of independent biometric measurements collected) and \( 1 \leq j \leq m \) (the number of scalar elements in each biometric measurement), \( \mu_i \) is the mean of the
3

\[ Y_i = \mu + \tau_i + \epsilon_{ij} \]  
Eq. 2

A simplifying assumption used here is that \( \epsilon_{ij} \) are mutually independent.

Further comments regarding notation: dot (e.g., \( Y'_i \)) means “add all the values of the subscript replaced with a dot,” and the bar (e.g., \( \bar{Y}_i \)) means “divide by the number of terms that have been added up (i.e., compute the average).” Finally, the standard deviation of a column-wise set of scalar measurements will be denoted as \( \sigma_{Y_i} \).

The mean of each measurement element in a sequence of biometric measurement vectors may be different. For example, consider the vectors obtained by recording key press times while a user types the password “Gamma 3” several times. These times are shown in Table 1 (all in milliseconds):

**TABLE 1**

<table>
<thead>
<tr>
<th>Trial</th>
<th>Element (1 ≤ i ≤ a)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(1 ≤ i ≤ m)</td>
</tr>
<tr>
<td>1</td>
<td>144</td>
</tr>
<tr>
<td>2</td>
<td>144</td>
</tr>
<tr>
<td>3</td>
<td>160</td>
</tr>
<tr>
<td>4</td>
<td>144</td>
</tr>
<tr>
<td>5</td>
<td>144</td>
</tr>
<tr>
<td>( \bar{Y}_i )</td>
<td>147.20</td>
</tr>
<tr>
<td>( \sigma_{Y_{ij}} )</td>
<td>7.16</td>
</tr>
</tbody>
</table>

The table shows that the “G” key is struck, on average, 147.20 ms after the “shift” key, and the first “a” keystroke occurs, on average, 204.80 ms after the “G.” (The first column, “shift,” is blank because that is the first key struck and serves only to mark the beginning of a trial.) Elements of other vectors of biometric measurements will also, in general, have different means. However, if the measurements are transformed as:

\[ Y_i = \frac{Y_i - \bar{Y}_i}{\sigma_{Y_{ij}}} \]  
Eq. 3

the measurements may be dealt with as random variables of zero mean and unit variance (standard normal variables). This transformation can be thought of as shifting the means of corresponding measurements to coincide at zero, and scaling the samples so that the variance of each set of corresponding samples is one. Thus transformed, the measurements can be treated more uniformly. For example, an estimate of sum of squares for errors is given by

\[ \text{sSE} = \sum_j \sum_i (Y_{ij} - \bar{Y}_i)^2 \]  
Eq. 4

and an estimate of mean square for error is given by

\[ \text{mse} = \frac{\text{sSE}}{m-n} \]  
Eq. 5

Similarly, the sum of squares of measurement elements is given by

\[ \text{ssL} = \sum_j m(Y_{ij} - \bar{Y}_i)^2 \]  
Eq. 6

and the mean square measurement is

\[ \frac{\text{ssL}}{n-1} \]  
Eq. 7

With these quantities defined, we can derive the upper confidence limit for \( \sigma^2 \) as

\[ P\left( \frac{\text{sSE}}{\sigma^2} \geq \chi^2_{m-n-1,\alpha} \right) = 1 - \alpha \]  
Eq. 8

where \( \chi^2_{m-n-1,\alpha} \) is the percentile of the chi-squared distribution with probability of \( 1 - \alpha \) in the right-hand tail, because

\[ \frac{\text{sSE}}{\sigma^2} \]  
follows the \( \chi^2 \) distribution. Replacing \( \text{sSE} \) by its observed value \( \text{ssE} \) (Eq. 4) gives a one-sided 100(1-\( \alpha \))% confidence bound for \( \sigma^2 \):

\[ \sigma^2 \leq \frac{\text{ssE}}{\chi^2_{m-n-1,\alpha}} \]  
Eq. 9

This is the upper bound for the error (\( \epsilon \)) variance.

This result is significant because it relates an important variable describing biometric identification system performance (\( \alpha \)) to the samples collected while enrolling a new user. Thus, it becomes possible to answer the questions, “given the samples collected, how can the system be expected to perform?” And conversely, “are the samples that have been collected consistent enough to achieve a desired level of performance?”

It is also possible to calculate the number of (additional) biometric measurements likely to be required to achieve tar-
get values for false reject ratio ("FRR" or "\(\alpha\)) and false accept ratio ("FAR" or "\(\beta\)"), given the variance (\(\sigma^2\)) of the samples already collected. Let \(\pi(\Delta) = (1-\beta)\) denote the power of the t-test at \(\Delta\), which is the probability of rejecting a hypothesis \(H_0: \{\tau_1, \ldots, \tau_n\}\) when at least two of the elements differ by \(\Delta\). Thus for given values of \(\Delta, \pi(\Delta), m, \) and \(\alpha,\) and variance \(\sigma^2\) of the data being collected, we can calculate how many more samples are needed.

Given a hypothesis \(H_0\) against \(H_1: \{\text{at least two } \tau_j\text{s differ}\}\) is by reject \(H_0\) if

\[
\frac{\text{msL}}{\text{msE}} > F_{m-1, n-m, \alpha}\]

If the null hypothesis is correct then

\[
\frac{\text{msL}}{\text{msE}}\]

has an F distribution, but if then null hypothesis is incorrect then

\[
\frac{\text{msL}}{\text{msE}}\]

has a non central F distribution \(F_{m-1, n-m, \delta^2}\) where the noncentrality parameter \(\delta^2\) is given by:

\[
\delta^2 = \frac{(m - 1)Q(\tau_j)}{\sigma^2} \quad \text{Eq. 10}\]

where

\[
Q(\tau_j) = \sum_{i=1}^{n} r_i \left( \tau_i - \sum_{k \neq i} r_k/\alpha \right) ^2 / (m - 1) \quad \text{Eq. 11}\]

Thus, when \(Q(\tau_j)=0\) then \(\delta^2=0\) and the distribution of

\[
\frac{\text{msL}}{\text{msE}}\]

becomes the F-distribution. If \(\delta^2>0\) then the mean and spread of the distribution of

\[
\frac{\text{msL}}{\text{msE}}\]

are larger than the usual F-distribution. For equal sample sizes \(r = r_1 = r_2 = \ldots = r_m\),

\[
\delta^2 = r \sum_{i=1}^{n} \frac{(\tau_i - \tau)^2}{\sigma^2}. \quad \text{Eq. 12}\]

Now let

\[
\mu + \tau_1 = \mu + \tau_2 = \ldots = \mu + \tau_{m-1} = c
\]

and

\[
\mu + \tau_1 = c + \frac{\Delta}{2}
\]

and

\[
\mu + \tau_m = c - \frac{\Delta}{2}
\]

for some constant \(c,\) then

\[
\delta^2 = r \sum_{i=1}^{n} \frac{(\tau_i - \tau)^2}{\sigma^2} = \frac{r \Delta^2}{2m \sigma^2}
\]

The power of the F-test depends on the sample size \(r\) through the distribution of

\[
\frac{\text{msL}}{\text{msE}}\]

which depends on \(\delta^2\). Since the power of the F-test is the probability of rejecting \(H_0,\) we have

\[
\Pi(\Delta) = P\left[ \frac{\text{msL}}{\text{msE}} > F_{m-1, n-m, \alpha}\right] \quad \text{Eq. 13}\]

The noncentral F can be found from standard tables of F distribution, which are tabulated with power \(\pi\) given as a function of

\[
\phi = \frac{\delta}{\sigma}
\]

for various values of \(v_1=m-1\) and \(v_2=n-m\) and \(\alpha,\)

Now,

\[
\Phi^2 = \frac{\delta^2}{m} = \frac{r \Delta^2}{2m \sigma^2}
\]

(substituting the value of \(\delta^2\) from Eq. 12), so

\[
r = \frac{2m \sigma^2 \Phi^2}{\Delta^2}
\]

\(r\) is the result of interest: it is the estimated number of biometric samples required to enroll the user to an expected level of accuracy. Practical implications of this result include that more samples should be collected if the number of samples collected so far is less than \(r.\) Also, the form of the equation confirms the intuitive hypotheses that the higher the variation \(\sigma^2\) in the collected samples, the more samples will be required, and that the larger the value of \(\Delta,\) the fewer samples will be needed.
Listing 1 shows a pseudo-code implementation of an algorithm for finding the required sample size given the variance of the already-collected samples and other parameters:

```
10 int
20 NumberOfSamplesRequired(A, H(A), m, n, a) {
30   VarianceUpperBound = \sigma^2 / \chi^2; /* From Eq. 9 */
40   v1 = n - 1;
50   v2 = 1000;  /* Initialize v1 to large value */
60   do {
70     \Phi = Lookup\PhiFromTable(\|\|\|, v1, v2);
80     \tau = round(2 * \|\|^2 * VarianceUpperBound * \Phi / \chi^2) + 1;
90     v2 = v1 * (\tau - 1);
100   } until (\tau converges or oscillates);
110   return \tau;
120 }
```

**Listing 1**

FIG. 2 outlines a practical application of the mathematical principles derived above. First, a plurality of biometric samples is collected (210). Embeddings may collect fingerprints, hand geometry measurements, iris or retina images, or (as considered in greater detail in the examples presented here) keystroke timing measurements. Next, an upper bound for the error variance is computed (220), and an estimated number of samples needed is calculated (230). These operations correspond to the functionality of the pseudo code shown in Listing 1. If the number of samples already collected equals or exceeds the estimated number (240), enrollment is complete. Otherwise, an embodiment may display the estimated number of samples still required to the user (250) via a numeric display, a "thermometer" graph, or some similar representation. A supplemental biometric sample of the same type is collected (260) and the computations (220, 230) are repeated over all the collected samples. Since the estimate of samples required to complete enrollment can be re-computed after each additional sample is collected and the enrollment process can be completed after enough statistically adequate samples are obtained, enrollment may be completed more quickly than a prior-art system that fixes a priori a required sample count and collects that number of samples before analyzing them to prepare a template.

The following paragraphs work a concrete example of an embodiment of the invention that uses keystroke latency timings (key-to-key delays as described above). The user is typing the string "phoh" to enroll. Nine samples were collected (raw data is shown in Table 2, and normalized latencies shown in Table 3) but, as the following calculations will show, only three are needed (so, using an embodiment of the invention, the sample collection could have terminated after collecting the third sample). A computation will also be shown using only the first three latencies (as if the user had only typed "phoh") to show the effect of a shorter biometric vector.

**TABLE 2-continued**

<table>
<thead>
<tr>
<th>Trial</th>
<th>Element (1 ≤ j ≤ 5)</th>
<th>(1 ≤ i ≤ 9)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>p</td>
<td>h</td>
</tr>
<tr>
<td>8</td>
<td>328</td>
<td>192</td>
</tr>
<tr>
<td>9</td>
<td>328</td>
<td>171</td>
</tr>
</tbody>
</table>

**TABLE 3**

<table>
<thead>
<tr>
<th>Normalized Element</th>
<th>Y_j − Y_\bar{j}</th>
<th>\sigma_{ij}</th>
</tr>
</thead>
<tbody>
<tr>
<td>Trial</td>
<td>p</td>
<td>h</td>
</tr>
<tr>
<td>1</td>
<td>1.360782</td>
<td>-0.729399</td>
</tr>
<tr>
<td>2</td>
<td>-0.94166</td>
<td>-0.141933</td>
</tr>
<tr>
<td>3</td>
<td>1.360782</td>
<td>-0.729399</td>
</tr>
<tr>
<td>4</td>
<td>0.625696</td>
<td>-0.766164</td>
</tr>
<tr>
<td>5</td>
<td>0.576972</td>
<td>1.564595</td>
</tr>
<tr>
<td>6</td>
<td>-0.94166</td>
<td>-0.141933</td>
</tr>
<tr>
<td>7</td>
<td>-0.15785</td>
<td>-0.141933</td>
</tr>
<tr>
<td>8</td>
<td>-0.94166</td>
<td>1.838556</td>
</tr>
<tr>
<td>9</td>
<td>-0.94166</td>
<td>-0.729399</td>
</tr>
</tbody>
</table>

**Table 4** shows the results of calculating ssE as described in relation to Eq. 4. No values are shown in the upper and left cells because a minimum of two samples (each with at least two normalized latencies) are required to decide whether more samples are required.

**TABLE 4**

<table>
<thead>
<tr>
<th>Trial</th>
<th>pho after typing:</th>
</tr>
</thead>
<tbody>
<tr>
<td>p</td>
<td>pho</td>
</tr>
<tr>
<td>1</td>
<td>1.042818</td>
</tr>
<tr>
<td>2</td>
<td>5.40517</td>
</tr>
<tr>
<td>3</td>
<td>6.04608</td>
</tr>
<tr>
<td>4</td>
<td>7.024777</td>
</tr>
<tr>
<td>5</td>
<td>9.155242</td>
</tr>
<tr>
<td>6</td>
<td>10.31425</td>
</tr>
</tbody>
</table>

**Table 5** gives the corresponding values or ssE, which are computed as ssE/(n−m) (Eq. 5) (blank rows and columns have been omitted); and the corresponding values of Chi-squared (\chi^2) (from statistical tables) are given on the right.

**TABLE 5**

<table>
<thead>
<tr>
<th>ssE for Second through Fifth Sample</th>
<th>phoh</th>
<th>phoha</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.871409</td>
<td>1.59235</td>
<td>3.12287627</td>
</tr>
<tr>
<td>1.831723</td>
<td>1.0155</td>
<td>1.16973513</td>
</tr>
<tr>
<td>1.653517</td>
<td>1.158416</td>
<td>1.470847617</td>
</tr>
<tr>
<td>1.440955</td>
<td>0.951686</td>
<td>1.15032809</td>
</tr>
<tr>
<td>1.53254</td>
<td>1.164823</td>
<td>1.22481933</td>
</tr>
<tr>
<td>1.473464</td>
<td>1.228168</td>
<td>1.22976669</td>
</tr>
</tbody>
</table>

**\chi^2**

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>0.103</td>
<td>0.352</td>
<td>0.711</td>
</tr>
<tr>
<td>0.711</td>
<td>1.635</td>
<td>2.733</td>
</tr>
<tr>
<td>1.635</td>
<td>3.325</td>
<td>5.226</td>
</tr>
<tr>
<td>2.733</td>
<td>5.226</td>
<td>7.902</td>
</tr>
</tbody>
</table>
TABLE 5-continued

<p>| | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>3.94</td>
<td>7.261</td>
<td>10.85</td>
<td></td>
</tr>
<tr>
<td>5.226</td>
<td>9.39</td>
<td>13.85</td>
<td></td>
</tr>
</tbody>
</table>

Table 6 gives the upper bound for $\sigma^2$ at 95% confidence level obtained by

$$\sigma^2 \leq \frac{sE}{X^2_{m,1-\alpha}}$$

Now, statistical tables of the power of the F-test, $\pi(\Phi)$ are consulted to find the value for $\Phi$. Those tables require values for $v_1$, the number of degrees of freedom, which in this case is simply $m-1$ or 3; $\alpha$, and $v_2$. We look for the desired power of the test (its discriminative power) and read off the corresponding value for $\Phi$ at the column head. As described in the algorithm of Listing 1, we begin with a large value for $v_2$ and successively approximate $r$ by setting $v_2$ for the next iteration to $m(r_{previous}) - 1$ until $r$ converges to a stable value or oscillates between two values (in the latter case, we select the smaller of the two values). Table 7 shows the power of the F-test for $v_1=3$ and $\alpha=0.01$:

| TABLE 7 |
|---|---|---|---|---|---|---|---|
| $v_2$ | 1.67 | 2.00 | 2.33 | 2.67 | 3.00 | 3.33 | 3.67 | 4.00 | 4.33 | 4.67 | 5.00 |
| 5 | 0.16 | 0.25 | 0.36 | 0.48 | 0.60 | 0.71 | 0.80 | 0.87 | 0.92 | 0.95 | 0.98 |
| 6 | 0.20 | 0.31 | 0.44 | 0.58 | 0.71 | 0.81 | 0.89 | 0.94 | 0.97 | 0.99 | 0.99 |
| 7 | 0.23 | 0.36 | 0.52 | 0.66 | 0.79 | 0.88 | 0.94 | 0.97 | 0.99 | 1.00 | 1.00 |
| 8 | 0.26 | 0.41 | 0.57 | 0.72 | 0.84 | 0.92 | 0.96 | 0.99 | 1.00 | 1.00 | 1.00 |
| 9 | 0.29 | 0.45 | 0.62 | 0.77 | 0.88 | 0.95 | 0.98 | 0.99 | 1.00 | 1.00 | 1.00 |
| 10 | 0.31 | 0.48 | 0.66 | 0.81 | 0.91 | 0.96 | 0.99 | 1.00 | 1.00 | 1.00 | 1.00 |
| 12 | 0.35 | 0.54 | 0.72 | 0.86 | 0.94 | 0.98 | 0.99 | 1.00 | 1.00 | 1.00 | 1.00 |
| 15 | 0.39 | 0.59 | 0.77 | 0.90 | 0.96 | 0.99 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| 20 | 0.44 | 0.65 | 0.83 | 0.93 | 0.98 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| 30 | 0.49 | 0.71 | 0.87 | 0.96 | 0.99 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| 60 | 0.55 | 0.77 | 0.91 | 0.97 | 0.99 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| 100 | 0.60 | 0.82 | 0.94 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| 1000 | 0.60 | 0.82 | 0.94 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |

TABLE 6

<table>
<thead>
<tr>
<th>mho</th>
<th>mho</th>
<th>mho</th>
</tr>
</thead>
<tbody>
<tr>
<td>18.16902</td>
<td>3.293282</td>
<td>1.846536747</td>
</tr>
<tr>
<td>2.576264</td>
<td>0.623548</td>
<td>0.428004072</td>
</tr>
<tr>
<td>1.011325</td>
<td>0.348315</td>
<td>0.281448071</td>
</tr>
<tr>
<td>0.527243</td>
<td>0.182106</td>
<td>0.144438936</td>
</tr>
<tr>
<td>0.38897</td>
<td>0.116022</td>
<td>0.111375017</td>
</tr>
<tr>
<td>0.281949</td>
<td>0.130797</td>
<td>0.08880698</td>
</tr>
</tbody>
</table>

With these foundational statistics computed, we proceed to calculate an estimate of the number of samples required to enroll the user successfully. This estimate is first computed after the second sample is collected, and may be re-computed after each additional sample, until the estimate is less than or equal to the total number of samples already in hand. In these calculations, we choose $\Delta=2\sigma$ (that is, if the variation is more than the $2\sigma$ of the already-collected samples then we need to take more samples). Since the data is standardized (i.e. $\sigma=1$), $\Delta=2.0$.

The estimate is given by Equation 14, reproduced here for convenience:

$$r = \frac{2m\sigma^2\Phi^2}{\Delta^2}$$

$\Delta$ is 4 because there are four latencies measured as the user types "mho" (p-to-h, h-to-o, o-to-h, and h-to-o). $\sigma^2$ is 1.846536747 (from Table 6) and $\Delta^2$ is 4 (because $\Delta$ was chosen to be 2.0).

For the first iteration, we calculate

$$r = \frac{2m\sigma^2\Phi^2}{\Delta^2} = \frac{2 \times 4 \times 1.85}{4} \Phi^2 = 3.7\Phi^2$$

Then, looking up the value for $\Phi$ that corresponds to our initial choice of $v_2=1000$, power of the test $= 0.99$ (highlighted triple border), we find $\Phi=2.67$ (bold). Substituting, we obtain

$$r = 3.7 \times (2.67)^2 = 26.38$$

or, rounding to the nearest integer larger (because it is not possible to take a fraction of a biometric sample), 27.

For the next iteration, we set

$$v_2 = m(r-1) = 4(26) = 104$$

then, interpolating from the values in Table 7 since there is no row for $v_2=104$, we might estimate a value for $\Phi$ of 2.95. This gives a second iteration result of $r=32.20$, and $v_2$ of 132.
Estimating $\Phi = 2.98$ gives $r = 52.85$, and $v_2$ of 132. Since $r$ has converged at 33, we estimate that—based on the two samples collected—a total of 33 samples will be required.

After collecting the next sample, however, we find that the variance $\sigma^2$ is 0.428004072 (Table 6). By repeating the iterative algorithm of Listing 1, we find that our estimate of samples required has dropped significantly, to only eight. The values of $v_2$, $\Phi$, and $r$ that occur during the processing of the third sample are shown in Table 8:

<table>
<thead>
<tr>
<th>Iteration</th>
<th>$v_2$</th>
<th>$\Phi$</th>
<th>$r$</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1000</td>
<td>2.67</td>
<td>6.10</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>24</td>
<td>3.10</td>
<td>8.22</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>32</td>
<td>3.00</td>
<td>7.70</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>28</td>
<td>3.00</td>
<td>7.70</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>28</td>
<td>3.00</td>
<td>7.70</td>
<td>$r$ has converged at 7.70 (rounded to 8)</td>
</tr>
</tbody>
</table>

As the sample collection progresses, $\sigma^2$ keeps shrinking because the typist is quite consistent, and after the fifth sample is obtained, the method indicates that “enough” samples have been collected. Table 9 shows the iterations performed for the fourth and fifth samples:

<table>
<thead>
<tr>
<th>Sample</th>
<th>$\sigma^2$</th>
<th>Iteration</th>
<th>$v_2$</th>
<th>$\Phi$</th>
<th>$r$</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>0.281448071</td>
<td>1</td>
<td>1000</td>
<td>2.67</td>
<td>4.01</td>
</tr>
<tr>
<td>5</td>
<td>0.144438936</td>
<td>1</td>
<td>1000</td>
<td>2.67</td>
<td>2.06</td>
</tr>
</tbody>
</table>

Repeating these calculations for the $\sigma^2$ values in the second column of Table 6 (i.e. the values that apply if the shorter string “pho” was being typed, $m=3$, $v_2=2$) we see that the estimates of samples required goes from 47 to 11 to 6 to 5, and the method indicates that “enough” samples have been collected after the fifth sample. Table 10, which follows the layout of Table 9, shows how the estimated number of samples required changes after each sample is collected. Note that the value for $\Phi$ must be looked up in a different table (i.e. not Table 7) because $m$ and $v_2$ are different in each example. The corresponding table for the power of the F-test for $v_2=2$, $\alpha=0.01$ is not reproduced here, but may be found in many statistics reference books.

<table>
<thead>
<tr>
<th>Sample</th>
<th>$\sigma^2$</th>
<th>Iteration</th>
<th>$v_2$</th>
<th>$\Phi$</th>
<th>$r$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>3.293282</td>
<td>1</td>
<td>1000</td>
<td>3.00</td>
<td>44.46</td>
</tr>
<tr>
<td>3</td>
<td>0.623548</td>
<td>1</td>
<td>1000</td>
<td>3.00</td>
<td>8.41</td>
</tr>
</tbody>
</table>

Note that in processing the fourth and fifth samples above, the iterative algorithm began oscillating between two values. The smaller of the two was selected in each case. Thus, after the fourth sample, 5.799 samples (rounded to six samples) were estimated to be required, while after the fifth sample, only 4.37 (5) samples were estimated to be required. Since five samples had already been collected, the enrollment process could have stopped.

This method uses the variability in a user’s keystroke patterns with desired FAR and FRR to arrive at sampling decisions. In an experiment with 43 users, this method resulted in sample size of six for 75% of the users and sample sizes varying from three to nine for the rest of the users. In this user population, a prior-art system would require at least nine samples from each user to be certain of successfully enrolling every user. However, by evaluating samples collected on the fly according to an embodiment of this invention, the majority of users could have enrolled with fewer samples.

The methods described above relate the number of biometric samples needed to achieve desired FRR and FAR ratios with the length of the number of characters needed in a password for keystroke authentication system. An algorithm based on this method can give an indication to give a user feedback on when he may stop giving biometric samples for authentication.

An embodiment of the invention can be implemented in a data processing system like the one shown in block-diagram form in FIG. 3. This system includes a programmable processor (a “central processing unit” or “CPU”) 305, memory 310, and mass storage device 315. A network interface 320 permits the system to communicate with other systems over a distributed data network. Other interfaces 325 (which may be built into the system or added as plug-in cards, as shown here) permit the system to communicate with various peripherals to collect biometric data. This system has an extensive complement of peripherals: a keyboard 330, mouse 335, fingerprint scanner 340, microphone 345, hand geometry sensor 350 and camera 355. Of course, systems with only one or two peripherals can also implement an embodiment of the invention.

A display 360 may be provided to present instructions, messages and other information to a user (not shown). Software instructions stored in memory 310 and executed by CPU 305, dedicated hardware circuitry, or a combination of hardware and software may be used to implement functions such as control logic 365 to coordinate the activities of other sub-systems and peripherals; biometric data collector 370 to operate a peripheral and take biometric measurements; statistics module 375 to analyze the collected biometric measurements according to the methods described earlier; and database 380 to store biometric templates constructed after user enrollment. Once a user has been enrolled, access control logic 385 may compare biometric data collected from a prospective user and compare it with a template stored in database 380 to
decide whether the prospective user should be granted access to a resource controlled by the system (not shown).

An embodiment of the invention may be a machine-readable medium having stored thereon instructions which cause a programmable processor to perform operations as described above. In other embodiments, the operations might be performed by specific hardware components that contain hard-wired logic. Those operations might alternatively be performed by any combination of programmed computer components and custom hardware components.

A machine-readable medium may include any mechanism for storing or transmitting information in a form readable by a machine (e.g., a computer), including but not limited to Compact Disc Read-Only Memory (CD-ROM), Read-Only Memory (ROM), Random Access Memory (RAM), and Erasable Programmable Read-Only Memory (EPROM).

The applications of the present invention have been described largely by reference to specific examples and in terms of particular allocations of functionality to certain hardware and/or software components. However, those of skill in the art will recognize that evaluation of biometric samples for their discriminative power can also be achieved by software and hardware that distribute the functions of embodiments of this invention differently than herein described. Such variations and implementations are understood to be captured according to the following claims.

1 claim:
1. A method comprising:
   collecting a plurality of biometric measurements of a person;
   computing a statistical measure based on the plurality of biometric measurements;
   while the statistical measure is less than a target value, collecting a supplemental biometric measurement of the person and updating the statistical measure based on the supplemental biometric measurement;
   storing a biometric template constructed from the plurality of biometric measurements and any supplemental biometric measurements;
   computing an estimate of a discriminative power of an F-test associated with a certain confidence of a biometric identification system based on the plurality of biometric measurements and any supplemental biometric measurements;
   calculating a number of supplemental measurements likely to be required to achieve target values for false rejection rate (FRR) and false acceptance rate (FAR); and
   calculating a number of supplemental measurements likely to be required to achieve target values for a certain confidence level.

2. The method of claim 1, wherein the statistical measure comprises an upper bound for an error variance.

3. The method of claim 1, further comprising:
   displaying the estimate of the discriminative power.

4. The method of claim 1, further comprising:
   computing an estimate of a number of supplemental biometric measurements required to complete enrollment; and
   displaying the estimate of a number of supplemental biometric measurements to the person.

5. The method of claim 4, wherein the number of supplemental biometric measurements required to complete enrollment is a plurality of supplemental measurements.

6. The method of claim 1, further comprising:
   comparing the candidate biometric measurement to the biometric template; and
   granting access to a resource to the candidate if the candidate biometric measurement matches the biometric template.

7. The method of claim 1 wherein each biometric measurement comprises a plurality of keystroke timing measurements collected while the person types on a keyboard.

8. The method of claim 1, wherein the number of supplemental measurements likely to be required to achieve target values for FRR and FAR is a plurality of supplemental measurements; and while the statistical measure is less than a target value, collecting a supplemental biometric measurement of the person and updating the statistical measure based on the supplemental biometric measurement; storing a biometric template constructed from the plurality of biometric measurements and any supplemental biometric measurements; and computing an estimate of a discriminative power associated with a certain confidence of a biometric identification system based on the plurality of biometric measurements and any supplemental biometric measurements; wherein
   the statistical measure is proportional to

\[
\frac{2mn^2\Phi^2}{\Delta^2}
\]

where

m is a number of elements in one biometric measurement,
\(\sigma^2\) is an upper bound for an error variance,
\(\Phi^2\) is a power of an F test, and
\(\Delta^2\) is a maximum allowable difference.

10. A non-transitory computer-readable medium containing instructions to cause a programmable processor to perform operations comprising:
   collecting a plurality of measurements of a characteristic of a user, each measurement including a plurality of scalar quantities;
   adjusting the plurality of measurements to produce standard normal variables;
   computing an estimate of a number of measurements required to achieve a target discriminative power associated with a certain confidence for a test, for a plurality of different numbers of elements that the measurements are related to;
   while a number of the plurality of measurements is less than the estimated number of measurements for all of the numbers of elements, collecting a supplemental measurement of the user and computing a new estimate of a number of measurements required to achieve the target discriminative power of the test based on the standard normal variables and the supplemental measurement; and
calculating a number of supplemental measurements likely 
to be required to achieve target values for false rejection 
rate (FRR) and false acceptance rate (FAR); and 
calculating a number of supplemental measurements likely 
to be required to achieve target values for a certain 
confidence level.

11. The computer-readable medium of claim 10 wherein 
computing is based on the standard normal variables.

12. The computer-readable medium of claim 10, contain-
ing additional instructions to cause the programmable pro-
cessor to perform operations comprising:

displaying the new estimate to the user.

13. The computer-readable medium of claim 10 wherein 
the characteristic of the user is a typing rhythm of the user.

14. The computer-readable medium of claim 10 wherein 
the characteristic of the user is a measurement of at least one 
of a hand geometry, a fingerprint, a retina image, or a voice 
recording.

15. A system comprising:
an input device to measure a characteristic of an enrolling 
user;
biometric sample collection logic to collect a plurality of 
measurements from the input device;
statistical analysis logic to compute a bounded estimate of 
a biometric identification capability based on the plurality 
of measurements;
control logic to cause the biometric sample collection logic 
to collect a supplemental measurement until the bounded estimate reaches a target value; and the control 
logic to compute an estimate of a discriminative power 
of an F-test associated with a certain confidence of a 
biometric identification system based on the plurality of 
biometric measurements and any supplemental biomet-
ric measurements;
the control logic to calculate a number of supplemental 
measurements likely to be required to achieve target 
values for false rejection rate (FRR) and false accep-
tance rate (FAR); and 
the control logic to calculate a number of supplemental 
measurements likely to be required to achieve target 
values for a certain confidence level.

16. The system of claim 15, further comprising:
a database to store a biometric template of the enrolling 
user prepared from the plurality of measurements and 
any supplemental measurements.

17. The system of claim 16, further comprising:
access control logic to perform a comparison of a biometric 
sample of a prospective user with the biometric template 
and grant access to a resource if the comparison indi-
cates that the prospective user is identical to the enroll-
ing user.

18. The system of claim 15 wherein the characteristic is a 
typing rhythm.

19. The system of claim 15, wherein the number of supple-
mental measurements likely to be required to achieve target 
values for FRR and FAR is a plurality of supplemental mea-
urements; and where the number of supplemental measure-
ments likely to be required to achieve target values for a 
certain confidence level is a plurality of supplemental measure-
ments.

20. A non-transitory computer-readable medium contain-
ing instructions to cause a programmable processor to per-
form operations comprising:

collecting a plurality of measurements of a characteristic of 
a user, each measurement including a plurality of scalar 
quantities;
adjusting the plurality of measurements to produce stand-
ard normal variables;
computing an estimate of a number of measurements 
required to achieve a target discriminative power associ-
cated with a certain confidence for a test, for a plurality 
of different numbers of elements that the measurements 
are related to; and
while a number of the plurality of measurements is less 
than the estimated number of measurements for all of the 
numbers of elements, collecting a supplemental mea-
surement of the user and computing a new estimate of a 
number of measurements required to achieve the target 
discriminative power of the test based on the standard 
normal variables and the supplemental measurement; 
wherein the number of supplemental measurements 
likely to be required to achieve target values for FRR and 
FAR is a plurality of supplemental measurements; and 
where the number of supplemental measurements likely 
to be required to achieve target values for a certain 
certainty level is a plurality of supplemental measure-
ments.

* * * * *